

- Every graph has an equation!

Lesson 20: Every Line Is a Graph of a Linear Equation

Classwork

Opening Exercise

Figure 1

use $y = mx + b$
 slope \downarrow \rightarrow y-int.

$y = \frac{2}{3}x - 3$

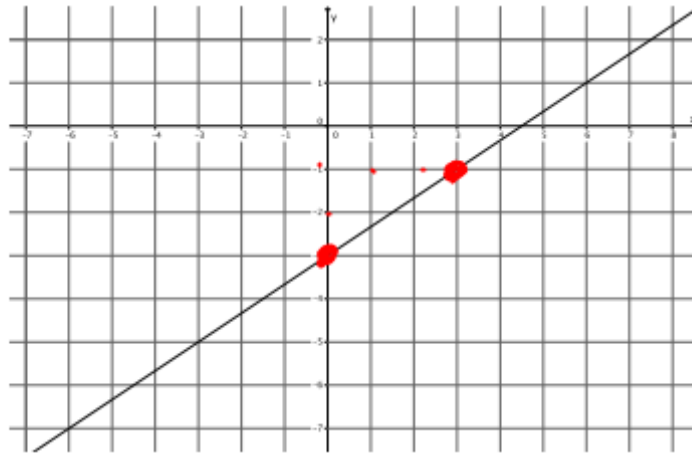
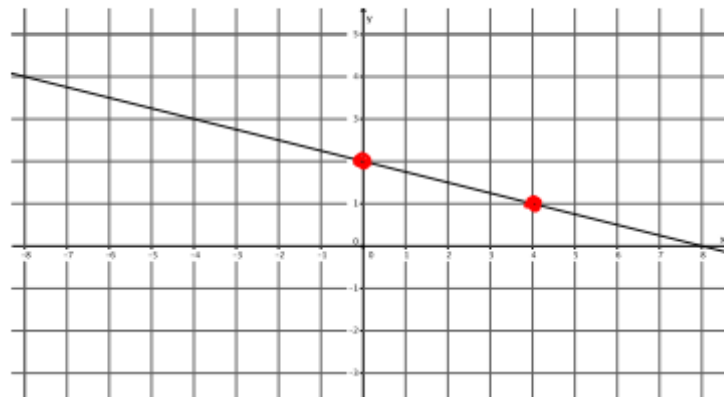


Figure 2

Slope = $\frac{\Delta y}{\Delta x}$



$y = -\frac{1}{4}x + 2$

Exercises

1. Write the equation that represents the line shown.

$$y = 3x + 2$$

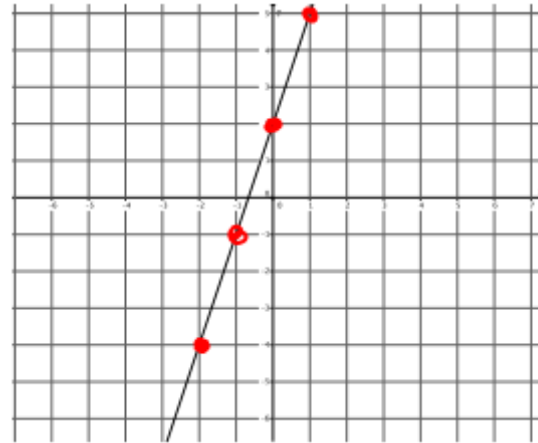
Use the properties of equality to change the equation from slope-intercept form, $y = mx + b$, to standard form, $ax + by = c$, where a , b , and c are integers, and a is not negative.

$$y = 3x + 2$$

$$-3x \quad | \quad -3x$$

$$-1 \quad (-3x + y = 2)$$

$$3x - y = -2$$



2. Write the equation that represents the line shown.

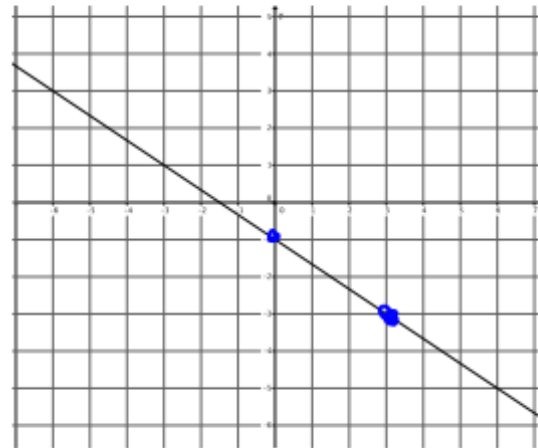
$$y = -\frac{2}{3}x - 1$$

Use the properties of equality to change the equation from slope-intercept form, $y = mx + b$, to standard form, $ax + by = c$, where a , b , and c are integers, and a is not negative.

$$y = -\frac{2}{3}x - 1$$

$$+\frac{2}{3}x \quad | \quad +\frac{2}{3}x$$

$$3 \left(\frac{2}{3}x + y = -1 \right)$$



$$\rightarrow 2x + 3y = -3$$

* Multiply by the common denominator *

3. Write the equation that represents the line shown.

$$y = -\frac{1}{5}x - 4$$

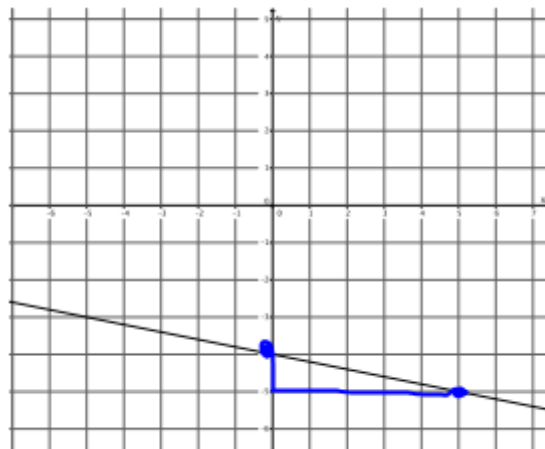
Use the properties of equality to change the equation from slope-intercept form, $y = mx + b$, to standard form, $ax + by = c$, where a , b , and c are integers, and a is not negative.

$$y = -\frac{1}{5}x - 4$$

$$+\frac{1}{5}x \cdot +\frac{1}{5}x$$

$$\left(\frac{1}{5}x + y = -4\right) \cdot 5$$

$$\rightarrow x + 5y = -20$$



4. Write the equation that represents the line shown.

$$y = x$$

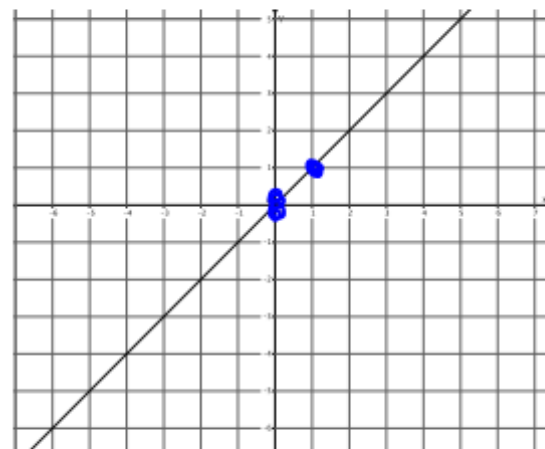
Use the properties of equality to change the equation from slope-intercept form, $y = mx + b$, to standard form, $ax + by = c$, where a , b , and c are integers, and a is not negative.

$$y = x$$

$$-x \quad -x$$

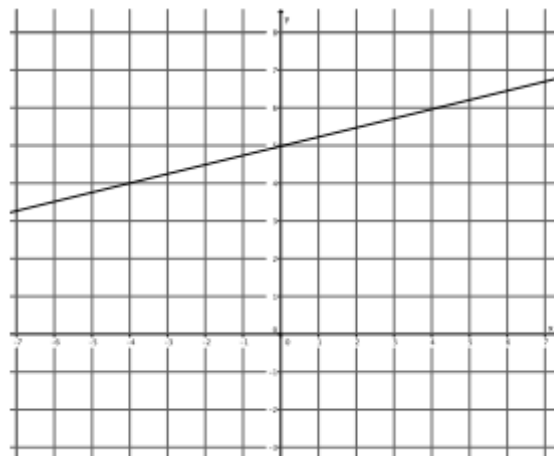
$$(-x + y = 0) \cdot -1$$

$$x - y = 0$$



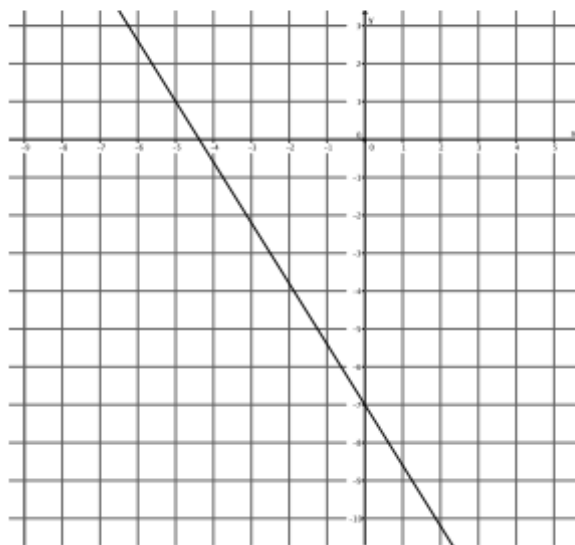
5. Write the equation that represents the line shown.

Use the properties of equality to change the equation from slope-intercept form, $y = mx + b$, to standard form, $ax + by = c$, where a , b , and c are integers, and a is not negative.



6. Write the equation that represents the line shown.

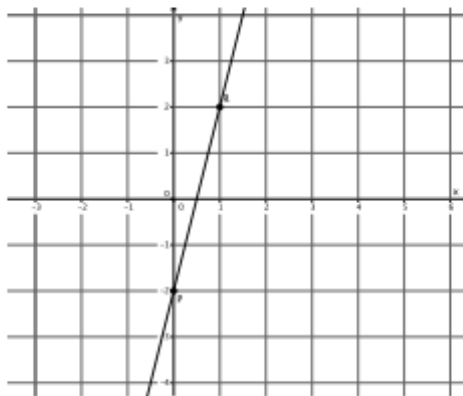
Use the properties of equality to change the equation from slope-intercept form, $y = mx + b$, to standard form, $ax + by = c$, where a , b , and c are integers, and a is not negative.



Lesson Summary

Write the equation of a line by determining the y -intercept, $(0, b)$ and the slope, m , and replacing the numbers b and m into the equation $y = mx + b$.

Example:



The y -intercept of this graph is $(0, -2)$.

The slope of this graph is $m = \frac{4}{1} = 4$.

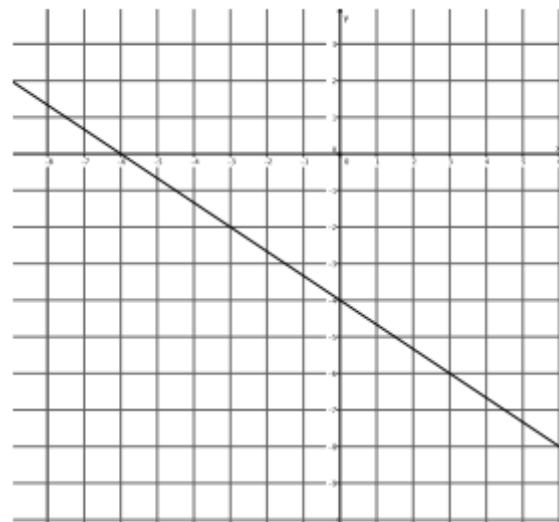
The equation that represents the graph of this line is $y = 4x - 2$.

Use the properties of equality to change the equation from slope-intercept form, $y = mx + b$, to standard form, $ax + by = c$, where a , b , and c are integers and a is not negative.

Problem Set

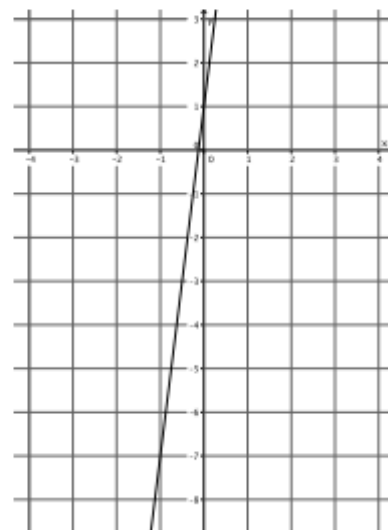
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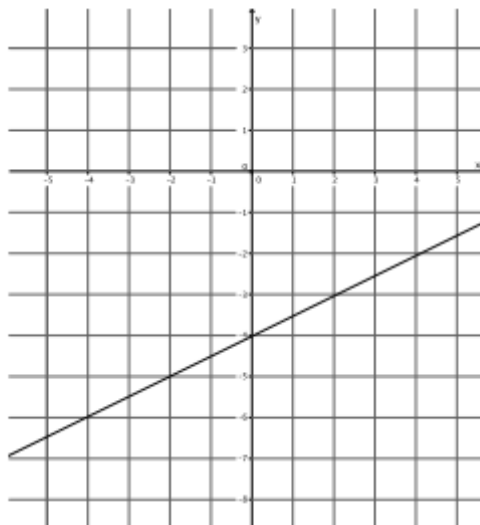
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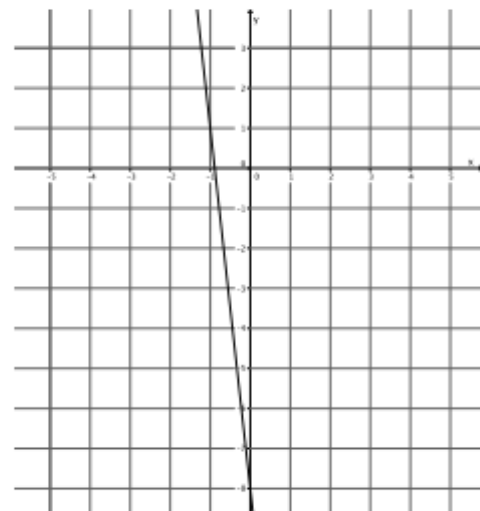
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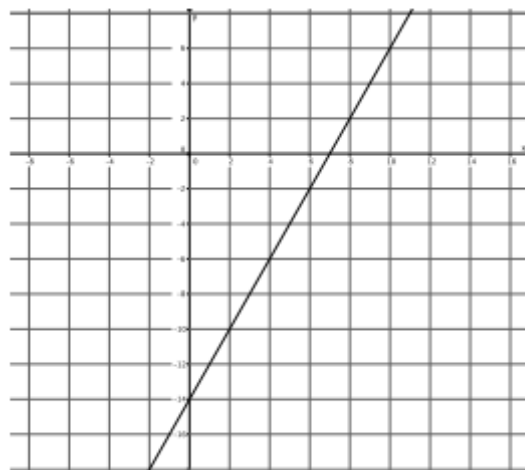
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